TYBSC, MATHS PAPER III (TOPOLOGY OF METRIC SPACE)
QUESTION BANKS (CONNECTEDNESS)

|  | Choose correct alternative in each of the following |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| 1 | Let ( $X, d$ ) be a finite metric space.If $A \subseteq X$ is connected then |  |  |  |
|  | (a) | $A=X$ | (b) | $A \neq X$ |
|  | (c) | $A$ is singleton set. | (d) | $A$ has more than one element. |
| 2 | If $A, B$ are connected subsets of $R$ with usual metric such that $A \cap B \neq \emptyset$, then |  |  |  |
|  | (a) | Only $A \cup B$ is connected. | (b) | Only $A \cap B$ is connected. |
|  | (c) | Both $A \cup B$ and $A \cap B$ are connected. | (d) | Only $A+B$ is connected. |
| 3 | If $A$ is connected subset of a metric space $X$ then......... is also connected. |  |  |  |
|  | (a) | $\underline{A}$ | (b) | Interior of $A$. |
|  | (c) | Both (a) and (b). | (d) | None of these. |
| 4 | An open ball in a metric space is ..... |  |  |  |
|  | (a) | Connected | (b) | Path connected |
|  | (c) | Both (a) and (b). | (d) | Compact. |
| 5 | Let $(X, d)$ be a connected metric space and $f: X \rightarrow Z$ be a continuous map. Then |  |  |  |
|  | (a) | $f$ is onto. | (b) | $f$ is one-one. |
|  | (c) | $f$ is bijective. | (d) | $f$ is constant. |
| 6 | A line is ........ |  |  |  |
|  | (a) | Convex. | (b) | Connected. |
|  | (c) | Path connected. | (d) | convex, connected, path connected |
| 7 | If $A$ is path connected subset of $R^{n}$ then which of the following set is not path connected. |  |  |  |
|  | (a) | $A^{0}$ | (b) | $\underline{A}$ |
|  | (c) | $\underline{A} \cup A$ | (d) | None of these. |
| 8 | The set $R^{2}-\{(x, y) / y=0\}$ is ..... |  |  |  |
|  | (a) | Path connected. | (b) | Connected. |
|  | (c) | Not connected. | (d) | Semi-closed. |
| 9 | The components of the set (0,1) $\cup\{2,3\}$ are ... |  |  |  |
|  | (a) | $(0,1)$ | (b) | \{2\},\{3\} |
|  | (c) | ( 0,1 ), \{2\} and $\{3\}$ | (d) | None of these. |
| 10 | If $A$ is connected subset of $Q$, with usual distance, then ... |  |  |  |
|  | (a) | $A=Q$ | (b) | $A$ is an infinite bounded set. |
|  | (c) | $A$ is singleton set. | (d) | None of these. |
| 11 | Metric space $R^{2} \backslash\{0\}$, with Euclidean metric,is ....... |  |  |  |
|  | (a) | Connected and path connected. | (b) | Connected but not path connected. |
|  | (c) | Neither connected nor path connected. | (d) | path connected but not connected. |


| 12 | Let $X$ be connected metric space and $Y$ be any metric space then the product space$X \times Y \ldots . .$ |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  | (a) | Is connected. | (b) | May not be connected. |
|  | (c) | Must be connected. | (d) | never connected |
| 13 | Every convex set is .. |  |  |  |
|  | (a) | Connected. | (b) | Path connected. |
|  | (c) | Both (a) and (b). | (d) | None of these. |
| 14 | Continuous image of a connected set is always ... |  |  |  |
|  | (a) | Path connected. | (b) | Not path connected. |
|  | (c) | Not connected. | (d) | None of these. |
| 15 | If a metric space $X$ can be written as union of two non-empty,disjoint and open sets then.. |  |  |  |
|  | (a) | $X$ is connected. | (b) | $X$ is separated. |
|  | (c) | $X$ is path connected. | (d) | None of these. |
| 16 | Every continuous function on a connected metric space to a set $\{-1,1\}$ is ..... |  |  |  |
|  | (a) | One-one. | (b) | Onto. |
|  | (c) | Bijective. | (d) | Constant. |
| 17 | Let $A, B$ and $C$ are subsets of a metric space $X$ such that $A \subseteq B \subseteq C$ and $A, C$ are connected then ..... |  |  |  |
|  | (a) | Set $B$ may not be connected. | (b) | Set $B$ is not connected. |
|  | (c) | Set $B$ is also connected. | (d) | None of these. |
| 18 | If $A, B$ are connected subsets of $R^{2}$ with Euclidean metric such that $A \cap B \neq \emptyset$, then |  |  |  |
|  | (a) | Both $A \cup B$ and $A \cap B$ are connected. | (b) | only $A \cup B$ is connected but $A \cap B$ need not be. |
|  | (c) | Only $A \cap B$ is connected but $A \cup$ $B$ need not be. | (d) | neither $A \cup B$ nor $A \cap B$ connected. |
| 19 | If $A, B$ are closed subsets of a metric space $X$ then $A \cap B^{c}$ is.... |  |  |  |
|  | (a) | Connected. | (b) | Closed. |
|  | (c) | Separated. | (d) | None of these. |
| 20 | If the characteristic function $\chi_{A}$ is continuous on a non-empty proper subset $A$ of metric space $X$ then.... |  |  |  |
|  | (a) | $X$ is not connected. | (b) | $X$ is connected. |
|  | (c) | $X$ is path connected. | (d) | X is compact. |
| 21 | $R^{n} \backslash\left\{0_{R^{n}}\right\}$ is not path connected if |  |  |  |
|  | (a) | $\mathrm{n}=3$ | (b) | $n=4$ |
|  | (c) | $\mathrm{n}=1$ | (d) | None of these. |
| 22 | The set $R^{2} \backslash Q \times Q$,Euclidean metric, is.... |  |  |  |
|  | (a) | Not connected. | (b) | Not path connected. |
|  | (c) | Connected. | (d) | None of these. |
| 23 | Let $(X, d)$ be a connected metric space and $f: X \rightarrow N$ be a continuous map. Then |  |  |  |
|  | (a) | $f$ is onto. | (b) | $f$ is one-one. |
|  | (c) | $f$ is bijective. | (d) | $f$ is constant. |


| 24 | The unit circle $S^{1}$, usual distance , is.... |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  | (a) | Compact and connected | (b) | Connected but not compact. |
|  | (c) | Compact but not connected. | (d) | Neither compact nor connected. |
| 25 | If $A, B$ are connected subsets of $R$ with usual metric such that $A \cap B \neq \varnothing$, then the following set may not be connected. |  |  |  |
|  | (a) | $A \cup B$ | (b) | $A \cap B$ |
|  | (c) | $A \backslash B$ | (d) | $A \times B$ in $R^{2}$ (Euclidean distance) |
| 26 | The component of the set $R \backslash Q$ is |  |  |  |
|  | (a) | An infinite set. | (b) | A set having more than one element. |
|  | (c) | A singleton set. | (d) | Having exactly two points. |

